### Additional file 1 relative percentage bias of parameter estimates in the path model at stage 2 (Equal sized studies)

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