The Bayesian gene sub-network example described in this Additional file corresponds to one gene node (Gene\(_j\)) with \((p - 1)\) parent genes (Gene\(_1\), Gene\(_2\), …, Gene\(_{p-1}\)). The joint probability density function for this sub-network composed of Gene\(_j\) and parent genes is described with a mixture of two multivariate Gaussian distributions \((k = 1, 2)\), each with a particular mean vector \((\mu_k)\) of dimension \(p\) and a variance-covariance matrix \((\Sigma_k)\) of dimension \(p \times p\). The genes of a network may exhibit different expression and co-expression patterns across the conditions under study. This situation is likely to be better described by more than one density (e.g. Gaussian) combined into a mixture model where each component receives a weight, rather than a single density. For example, a gene (e.g. Gene\(_2\)) may have a strong influence on the expression of another gene (e.g. Gene\(_j\)) under certain conditions, and this strong association is better described by one mixture component. The influence of the former gene may be weak under another set of
conditions, and this weak association is better described by a different mixture component. The correlation $\rho_{jq}$ between the Gene$_q$ ($Gene_q \in a(Gene_j)$) and Gene$_j$ within a mixture component is a function of the covariance and variance estimates that correspond to the off-diagonal and diagonal entries of $\Sigma$, weighted by the component weight $\alpha_k$. 